

## Some preliminary-analysis regression models for the CRT-motivated cognition study

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<b>Ordered logit estimates</b>  <b>Log likelihood = -1804.1615</b>	<table style="width: 100%; border-collapse: collapse;"> <tr> <td style="text-align: right;">Number of obs</td> <td style="text-align: left;">=</td> <td style="text-align: right;">1700</td> </tr> <tr> <td style="text-align: right;">LR chi 2(1)</td> <td style="text-align: left;">=</td> <td style="text-align: right;">9.73</td> </tr> <tr> <td style="text-align: right;">Prob &gt; chi 2</td> <td style="text-align: left;">=</td> <td style="text-align: right;">0.0018</td> </tr> <tr> <td style="text-align: right;">Pseudo R2</td> <td style="text-align: left;">=</td> <td style="text-align: right;">0.0027</td> </tr> </table>	Number of obs	=	1700	LR chi 2(1)	=	9.73	Prob > chi 2	=	0.0018	Pseudo R2	=	0.0027
Number of obs	=	1700											
LR chi 2(1)	=	9.73											
Prob > chi 2	=	0.0018											
Pseudo R2	=	0.0027											

crt	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
dem_repub	.0673146	.0216044	3.12	0.002	.0249708	.1096584
__cut1	.7219973	.0981374	(Ancillary parameters)			
__cut2	1.639566	.1052953				
__cut3	2.870942	.1294138				

Regression model used to estimate impact of partisan self-identification on CRT score. “Dem\_repub” is standard 7-point measure of party affiliation.

<b>Ordered logit estimates</b>  <b>Log likelihood = -1837.7757</b>	<table style="width: 100%; border-collapse: collapse;"> <tr> <td style="text-align: right;">Number of obs</td> <td style="text-align: left;">=</td> <td style="text-align: right;">1750</td> </tr> <tr> <td style="text-align: right;">LR chi 2(1)</td> <td style="text-align: left;">=</td> <td style="text-align: right;">27.24</td> </tr> <tr> <td style="text-align: right;">Prob &gt; chi 2</td> <td style="text-align: left;">=</td> <td style="text-align: right;">0.0000</td> </tr> <tr> <td style="text-align: right;">Pseudo R2</td> <td style="text-align: left;">=</td> <td style="text-align: right;">0.0074</td> </tr> </table>	Number of obs	=	1750	LR chi 2(1)	=	27.24	Prob > chi 2	=	0.0000	Pseudo R2	=	0.0074
Number of obs	=	1750											
LR chi 2(1)	=	27.24											
Prob > chi 2	=	0.0000											
Pseudo R2	=	0.0074											

crt	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
Zreligiosity	-.2492808	.0477889	-5.22	0.000	-.3429454	-.1556163
__cut1	.4859958	.0495981	(Ancillary parameters)			
__cut2	1.412115	.0604305				
__cut3	2.637241	.0951115				

Regression model used to estimate impact of religiosity on CRT score. Zreligiosity is a composite Likert measure formed by aggregation of church attendance, importance of God, and importance of prayer.

```
. ologit crtbias x_conservrepub skeptic_biased nonskeptc_biased
```

```
Iteration 0: log likelihood = -2885.4327
Iteration 1: log likelihood = -2885.7451
Iteration 2: log likelihood = -2885.7417
Iteration 3: log likelihood = -2885.7417
```

```
Ordered logistic regression      Number of obs   =    1577
                                LE chi2(3)          =    15.98
                                Prob > chi2          =    0.0015
                                Pseudo R2           =    0.0029
```

```
Log likelihood = -2885.7417
```

crtbias	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
x_conservr-b	-.1836118	.0451196	-3.83	0.000	-.2520445	-.075179
skeptc_bi-d	-0.075998	.1092246	-0.70	0.487	-.2900742	.1380782
nonskeptc-d	-.1682204	.1087078	-1.55	0.122	-.3812857	.0448429
/cut1	-1.001457	.0841236			-1.166816	-.8385575
/cut2	-3.772476	.0802301			-3.945134	-.2198819
/cut3	.3848447	.0802316			.2277761	.5420133
/cut4	1.417287	.0892902			1.242281	1.592292
/cut5	2.403202	.1122798			2.183139	2.623264

```
. est store M1
```

```
. ologit crtbias x_conservrepub skeptic_biased nonskeptc_biased x_conservrep
```

```
> uh_x_skeptc x_conservrepub x_nonskeptc
Iteration 0: log likelihood = -2893.4327
Iteration 1: log likelihood = -2848.1754
Iteration 2: log likelihood = -2848.0475
Iteration 3: log likelihood = -2848.0474
```

```
Ordered logistic regression      Number of obs   =    1577
                                LE chi2(5)          =    90.77
                                Prob > chi2          =    0.0000
                                Pseudo R2           =    0.0189
```

```
Log likelihood = -2848.0474
```

crtbias	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]
x_conservr-b	-1.1304747	.0797148	-1.84	0.102	-.2887127 0.0257634
skeptc_bi-d	-.0855652	.1098194	-0.78	0.438	-.3008072 0.1298768
nonskeptc-d	-1.1587811	.1090117	-1.44	0.150	-.3704401 0.0588779
x_conservr..	-.5452478	.1128249	-4.83	0.000	-.7663805 .324115
x_conservr..	.4119097	.1107427	3.72	0.000	.1948579 .6289615
/cut1	-1.039484	.0850675			-1.206214 - .8727552
/cut2	-.3937902	.0808728			-.5522975 - .2352828
/cut3	.3967532	.0809362			.2381172 .5553801
/cut4	1.462296	.0905793			1.285128 1.640192
/cut5	2.466436	.1138269			2.24334 2.689533

```
. est store M2
```

```
. lrtest M1 M2
```

```
Likelihood-ratio test      LE chi2(2) =    75.39
(Assumption: M1 nested in M2) Prob > chi2 =    0.0000
```

```
Iteration 0: log likelihood = -2893.4327
Iteration 1: log likelihood = -2848.0869
Iteration 2: log likelihood = -2848.8555
Iteration 3: log likelihood = -2848.8554
```

```
Ordered logistic regression
```

```
Number of obs   =    1577
LE chi2(9)      =    98.15
Prob > chi2     =    0.0000
Pseudo R2      =    0.0173
```

```
Log likelihood = -2848.8554
```

	crtbias	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
x_conservr-b		-.1392897	.0800888	-1.74	0.082	-.2982382	.0177043
skeptc_bi-d		-.082243	.1102055	-0.73	0.458	-.2982418	.1337558
nonskeptc-d		-.1450981	.1093739	-1.33	0.185	-.3594548	.0692598
x_conservr..		.5433568	.1131357	4.80	0.000	.7850988	.3216149
x_conservr..		.413895	.1109903	3.73	0.000	.1983579	.631432
x_crt		.0455212	.0741232	0.61	0.539	-.0975777	.1908
x_crm-x_crt		.059763	.0435584	1.37	0.170	-.0256099	.1451369
x_crt_x_alb-c		.0331948	.1084553	0.30	0.767	-.2447032	.1804337
x_crt_x_no-c		-.0821478	.105674	-0.59	0.556	-.2892548	.1449696
/cut1		-1.033639	.085284			-1.200993	-.866856
/cut2		-.3875913	.0811542			-.5488505	-.2285321
/cut3		.4034996	.0812484			.2445357	.5627456
/cut4		1.486799	.0908909			1.291675	1.677821
/cut5		2.473985	.1140883			2.250086	2.697304

```
. est store M3
```

```
. lrtest M2 M3
```

```
Likelihood-ratio test      LE chi2(4) =    2.38
(Assumption: M2 nested in M3) Prob > chi2 =    0.6655
```

```
. ologit crtbias x_conservrepub skeptic_biased nonskeptc_biased x_conservrep
> uh_x_skeptc x_conservrepub x_nonskeptc x_crt x_conservrepub x_crt x_crt_x_alb-c x_crt_x_no-c
> /c/*
*/ x_conservrepub x_crt_x_alb-c x_conservrepub x_crt_x_no-c
```

```
Iteration 0: log likelihood = -2893.4327
Iteration 1: log likelihood = -2841.709
Iteration 2: log likelihood = -2841.5437
Iteration 3: log likelihood = -2841.5437
```

```
Ordered logistic regression
```

```
Number of obs   =    1577
LE chi2(11)     =    103.78
Prob > chi2     =    0.0000
Pseudo R2      =    0.0185
```

```
Log likelihood = -2841.5437
```

	crtbias	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
x_conservr-b		-.1277481	.0802154	-1.59	0.111	-.2848673	.0294711
skeptc_bi-d		-.0839899	.1102853	-0.76	0.448	-.290109	.1321183
nonskeptc-d		-.1418057	.1094285	-1.30	0.195	-.3562816	.0728702
x_conservr..		-.5477638	.1135018	-4.83	0.000	-.7702231	-.3253044
x_conservr..		.3875037	.1113971	3.48	0.001	.1686984	.6054381
x_crt		.0435788	.0738404	0.59	0.555	-.1011457	.1883033
x_crm-x_crt		-.0505905	.0725755	-0.69	0.488	-.194141	.0922531
x_crt_x_alb-c		-.0358234	.108357	-0.33	0.742	-.2478993	.1787525
x_crt_x_no-c		.0333882	.1058518	0.32	0.752	-.2408549	.1740788
x_conservr..		.0167562	.107618	0.16	0.878	-.1841713	.2273836
x_crt_x_non		.3061852	.1043125	2.94	0.003	.1017364	.510634
/cut1		-1.04389	.0854218			-1.211313	-.8764059
/cut2		-.3963504	.0812744			-.5556452	-.2370556
/cut3		.3984148	.0813438			.2389838	.5578455
/cut4		1.47189	.0910539			1.293428	1.650353
/cut5		2.481872	.1143649			2.257521	2.705833

```
. est store M4
```

```
. lrtest M3 M4
```

```
Likelihood-ratio test      LE chi2(2) =    10.62
(Assumption: M3 nested in M4) Prob > chi2 =    0.0049
```

Regression model used to test experimental hypotheses and estimate graphically presented experimental effects. Variables are entered in stages. In the first, Zconserv\_repub (a composite Likert scale formed by combining the 5-point liberal-conservative ideology measure and the 7-point party-self-identification measure) is shown to predict disagreement with the proposition that CRT is a valid measure controlling for experimental condition (i.e., as subjects become more Republican and more conservative, they are more likely to disagree). In model 2, cross-product interaction terms are added. The show that the impact of being Republican and conservative predicts greater likelihood of disagreement, and being Democrat and liberal greater likelihood of agreement, in the “skeptc-biased” condition relative to the control; and that those effects are reversed in the “non-skeptc biased” condition. (Note Chris Mooney & friends: the model assumes the impact of the experimental assignment is linear with respect to ideology/party affiliation; you can’t tell from the model—you have to test a polynomial fit to figure out if there is asymmetry! I haven’t seen that done in the literature. I’ll do it in next post w/ this data in next post!). Model 3 adds CRT and also CRT x experimental treatment interaction terms; CRT score does not predict the disposition to see the CRT test as a valid measure of reflection and open-mindedness—in any of the conditions—independently of ideology. But there is a CRT-ideology/party interaction. That’s what model 4 shows by adding 3-way interactions for party/ideology, CRT, and experimental treatment. There is a significant 3-way interaction effect – you can see that by looking at the Likelihood Ratio test (G-statistic), which confirms that the addition of the variables in model 4 added a statistically significant increment of explanatory power. But 3-way interactions are hard to interpret w/o graphic data illustration—which I supply in the post.